HONG KONG EXAMINATIONS AUTHORITY

HONG KONG CERTIFICATE OF EDUCATION EXAMINATION 2001

## MATHEMATICS PAPER 1

**Question-Answer Book** 

8.30 am - 10.30 am (2 hours)
This paper must be answered in English

- Write your Candidate Number, Centre Number and Seat Number in the spaces provided on this cover.
- 2. This paper consists of THREE sections, A(1), A(2) and B. Each section carries 33 marks.
- 3. Attempt ALL questions in Sections A(1) and A(2), and any THREE questions in Section B. Write your answers in the spaces provided in this Question-Answer Book. Supplementary answer sheets will be supplied on request. Write your Candidate Number on each sheet and fasten them with string inside this book.
- 4. Write the question numbers of the questions you have attempted in Section B in the spaces provided on this cover.

Total

- 5. Unless otherwise specified, all working must be clearly shown.
- 6. Unless otherwise specified, numerical answers should be either exact or correct to 3 significant figures.
- The diagrams in this paper are not necessarily drawn to scale.

Section A	13	12	11	10	8–9	7	5–6	3-4	1–2	Section A Question No.			Seat Number	Centre Number	Candidate Number	
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										Marks	Examiner No.	Examiner's Use Only				

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	Section A Total

Section B Total	·	Section B Question No.*
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<sup>\*</sup>To be filled in by the candidate.

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◎香港考試局



## FORMULAS FOR REFERENCE

	$\frac{1}{3}$ × base area × height	П	Volume	PYRAMID
	base area × height	II	Volume	PRISM
	$\frac{1}{3}\pi r^2 h$	H	Volume	
	$\pi r l$	II	Area of curved surface	CONE
ş	$\pi r^2 h$	11	Volume	
	$2\pi rh$	П	Area of curved surface	CYLINDER
	$\frac{4}{3}\pi r^3$	II	Volume	
	$4\pi r^2$	11	Surface area	SPHERE

SECTION A(1) (33 marks) Answer ALL questions in this section and write your answers in the spaces provided.

2. Le	1. Sii
t f(x) =	nplify
$x^3-x^2$	Simplify $\frac{m}{(mn)^2}$ and express your answer with positive indices.
+x-1	and exp
. Find t	oress yo
Let $f(x) = x^3 - x^2 + x - 1$ . Find the remainder when $f(x)$ is divided by $x - 2$ .	ur answ
inder wł	er with <sub>l</sub>
nen f(x)	positive
is divi	indices.
ded by	
x-2.	
(3 marks)	(3 marks)

(3 marks)

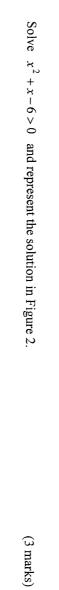
 $\dot{n}$ Find the perimeter of the sector in Figure 1.

3 cm $\int_{2^{\circ}}$ 

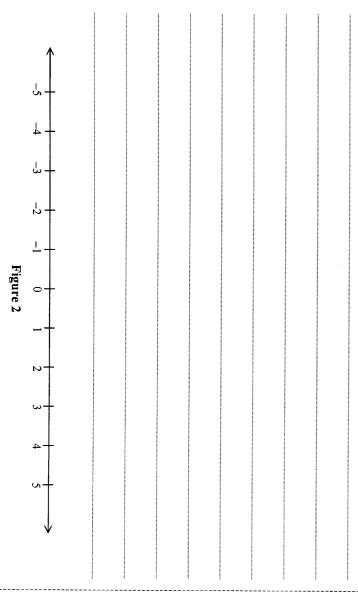
Figure 1







4.



(4 marks)



ċ In Figure 3, AC is a diameter of the circle. Find  $\angle DAC$ .

/30° \°•

Figure 3

Make x the subject of the formula  $y = \frac{1}{2}(x+3)$ . (4 marks)

6.

If the value of y is increased by 1, find the corresponding increase in the value of x.

(4 marks)

Two points A and B are marked in Figure 4.

7.

(a) Write down the coordinates of A and B.

(b) Find the equation of the straight line joining A and B.

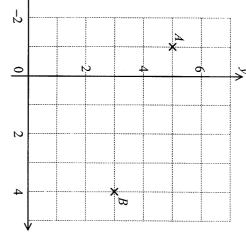
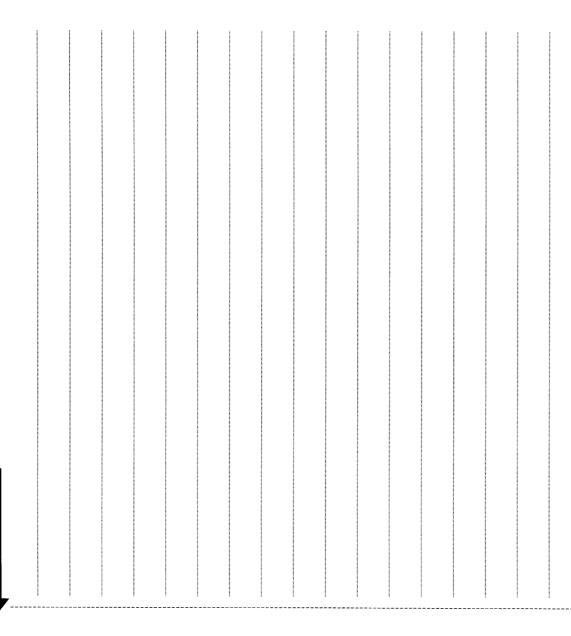


Figure 4



(4 marks)	Page total



8. The price of a textbook							9. In Figure 5, find $AB$ and the area of $\triangle ABC$ .	8 cm		A Figure	A Figure 5		
The price of a textbook was \$80 last year. The price is increased by 20% this year.	Peter is given a 20% discount when buying the textbook from a bookstore this year. How much does he pay for this book?						nd the area of $\Delta ABC$ .		B				
% this year.	ookstore this year.		:										
(4 marks)		***************************************					(5 marks)		***************************************				

## Section A(2) (33 marks)

Answer ALL questions in this section and write your answers in the spaces provided.

10. The histogram in Figure 6 shows the distribution of scores of a class of 40 students in a test.

Frequency 15 Distribution of scores of 40 students

0 40 6 Figure 6 Score 70

Table 1 Frequency distribution table for the scores of 40 students

	68 ≤ <i>x</i> < 76		$52 \le x < 60$	$44 \le x < 52$	Score (x)
80		64			Class mid-value (Class mark)
	11	15		ω	Frequency

(a) Complete Table 1.

(3 marks)

9 Estimate the mean and standard deviation of the distribution.

(2 marks)

<u>o</u> Susan scores 76 in this test. Find her standard score

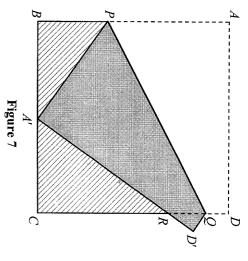
(2 marks)

<u>a</u>

test. Another test is given to the same class of students. It is found that the mean and standard deviation of the scores in this second test are 58 and 10 respectively. Relative to her classmates, if Susan performs equally well in these two tests, estimate her score in the second It is found that the mean and standard and 10 respectively partial (2 marks)



- 1 As shown in Figure 7, a piece of square paper ABCD of side 12 cm is folded along a line segment PQ so that the vertex A coincides with the mid-point of the side BC. Let the new positions of Aand D be A' and D' respectively, and denote by R the intersection of A'D' and CD.
- (a) Let the length of AP be x cm. By considering the triangle PBA', find x. (3 marks) (3 marks)



**(b)** Prove that the triangles PBA' and A'CR are similar. (3 marks)

- <u>o</u> Find the length of A'R. (2 marks)



12.  $F_1, F_2, F_3, \cdots, F_{40}$  as shown below are 40 similar figures. The perimeter of  $F_1$  perimeter of each succeeding figure is 1 cm longer than that of the previous one. is 10 cm. The



- (a) (i) Find the perimeter of  $F_{40}$ .
- (ii) Find the sum of the perimeters of the 40 figures.

(4 marks)

- (b) It is known that the area of  $F_1$  is  $4 \text{ cm}^2$ .
- (i) Find the area of  $F_2$ .
- $\Xi$ sequence? Determine with justification whether the areas of  $F_1, F_2, F_3, \dots, F_{40}$  form an arithmetic (4 marks)

Page total



13. S is the sum of two parts. One part varies as t and the other part varies as the square of t. The table below shows certain pairs of the values of S and t.

<b>1</b> 0 1	S = 0 33
2	56
ယ	69
4	72
S	65
6	48
7	21

(a) Express S in terms of t.

(3 marks)

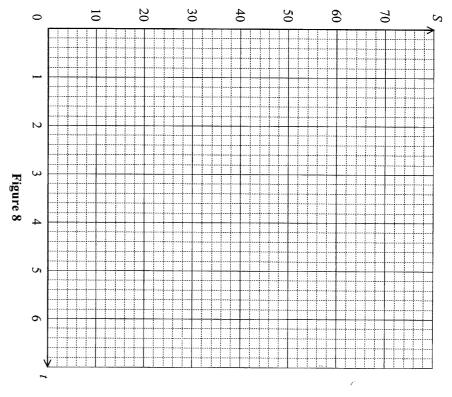
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(b) Find the value(s) of t when S = 40.

(2 marks)

		***************************************

<u>O</u> Using the data given in the table, plot the graph of S against t for  $0 \le t \le 7$  in Figure 8.



Read from the graph the value of t when the value of S is greatest.

(3 marks)

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## SECTION B (33 marks)

Answer any THREE questions in this section and write your answers in the spaces provided. Each question carries 11 marks.

- 14. (a) Let  $f(x) = x^5 6x + 5$ . (i) Complete Table 2.
- (ii) It is known that the equation f(x) = 0 has only one root greater than 1. Using
  (i) and the method of bisection, find this root correct to 3 decimal places.
  (5 marks)

1.15	1.1	1.05	<b>—</b>	X
0.111		. 432	<i>y</i> 0	(x)

**(b)** From 1997 to 2000, Mr. Chan deposited \$1000 in a bank at the beginning of each year at an interest rate of r% per annum, compounded yearly. For the money deposited, the amount accumulated at the beginning of 2001 was \$5000. Using (a), find r correct to 1 decimal place. (6 marks)

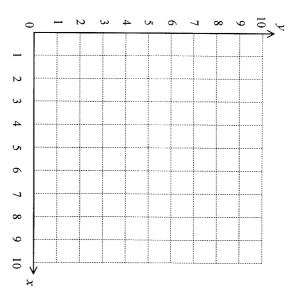
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15. (a) In Figure 9, shade the region that represents the solution to the following constraints:

$$\begin{cases} 1 \le x \le 9, \\ 0 \le y \le 9, \\ 5x - 2y > 15. \end{cases}$$

(4 marks)



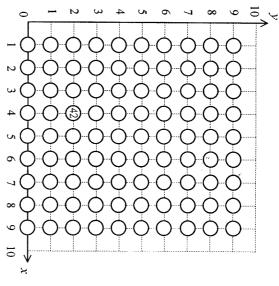


Figure 9

Figure 10

9 marked in the figure as an illustration. A restaurant has 90 tables. Figure 10 shows its floor plan where a circle represents a table. Each table is assigned a 2-digit number from 10 to 99. A rectangular coordinate system is introduced to the floor plan such that the table numbered 10x + y is located at (x, y) where xis the tens digit and y is the units digit of the table number. The table numbered 42 has been

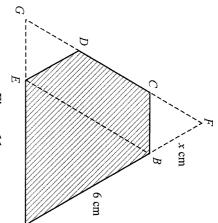
area. The restaurant is partitioned into two areas, one smoking and one non-smoking. Only those tables with the digits of their table numbers satisfying the constraints in (a) are in the smoking

- $\Xi$ In Figure 10, shade all the circles which represent the tables in the smoking area
- $\Xi$ Two tables are randomly selected, one after another and without replacement from the tables. Find the probability that 90
- (I) the first selected table is in the smoking area;
- $\Xi$ smoking area and its number is a multiple of 3. of the two selected tables, one is in the smoking area, and the other is in the non-

(7 marks)



16. and the area of BCDE is  $5\sqrt{3}$  cm<sup>2</sup>. Figure 11 shows a piece of pentagonal cardboard ABCDE. It is formed by cutting off two equilateral triangular parts, each of side x cm, from an equilateral triangular cardboard AFG. AB is 6 cm long



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Figure 11

Figure 12

(a) Show that  $x^2 - 12x + 20 = 0$ .

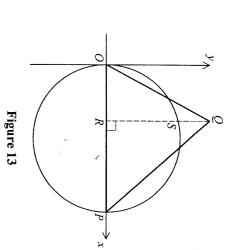
Hence find x.

(4 marks)

- 9 The triangular part ABE in Figure 11 is folded up along the line BE until the vertex A comes to the position A' (as shown in Figure 12) such that  $\angle A'ED = 40^{\circ}$ .
- (i) Find the length of A'D.
- (ii) Find the angle between the planes BCDE and A'BE.
- (iii) If A', B, C, D, E are the vertices of a pyramid with base BCDE, find the volume of the pyramid. (7 marks)



- 17. (a) In Figure 13, OP is a diameter of the circle. The altitude QR of the acute-angled triangle OPQ cuts the circle at S. Let the coordinates of P and S be (p,0) and (a,b) respectively.
- (i) Find the equation of the circle *OPS*.
- (ii) Using (i) or otherwise, show that  $OS^2 = OP \cdot OQ \cos \angle POQ$ . (7 marks)



9

In Figure 14, ABC is an acute-angled triangle. AC and BC are diameters of the circles AGDC and BCEF respectively.

- (i) Show that BE is an altitude of  $\triangle ABC$ .
- (ii) Using (a) or otherwise, compare the length of *CF* with that of *CG*.

  Justify your answer.

(4 marks)

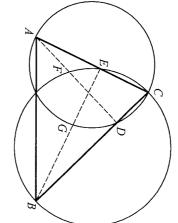


Figure 14

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