

S.5 Mock Exam. (2001-2002)

Mathematics. Paper (II).

$$1. \quad x = \frac{ab}{1+a+b}.$$

$$x(1+a+b) = ab.$$

$$x + ax + bx = ab.$$

$$x(1+b) = ab - ax$$

$$x(1+b) = a(b-x)$$

$$a = \frac{x(1+b)}{b-x}. \quad (C)$$

$$2. \quad x \xrightarrow{-30\%} 0.7x \xrightarrow{+r\%} x.$$

$$0.7x(1+r\%) = x.$$

$$(1+r\%) = \frac{1}{0.7}$$

$$1+r\% = 1.4286.$$

$$r\% = 0.4286$$

$$r\% = 42.86\%. \quad (D)$$

$$3. \quad y \xrightarrow{+40\%} x \xrightarrow{-20\%} z$$

$$x = (1+40\%)y$$

$$= 1.4y.$$

$$z = 1.4y(1-20\%)$$

$$= 1.12y.$$

$$\therefore y : z$$

$$= y : 1.12y$$

$$= 1 : 1.12$$

$$(D)$$

$$4. \quad \sqrt{x \sqrt{x \sqrt{x}}}$$

$$= [x(x(x^{\frac{1}{2}}))^{\frac{1}{2}}]^{\frac{1}{2}}$$

$$= [x(x^{\frac{3}{2}})^{\frac{1}{2}}]^{\frac{1}{2}}$$

$$= [x \cdot x^{\frac{3}{4}}]^{\frac{1}{2}}$$

$$= (x^{\frac{7}{4}})^{\frac{1}{2}} = x^{\frac{7}{8}} \quad (B)$$

$$5. \quad \frac{(a^n)^n \cdot a^{n+1}}{a^{-n}}$$

$$= \frac{a^{n^2} \cdot a^{n+1}}{a^{-n}}$$

$$= a^{n^2+n+1-(n)} = a^{n^2+2n+1}$$

$$= a^{(n+1)^2} = a^{(n+1)^2} \quad (A)$$

$$6. \quad (p-1)x^2 - 2x + 1 = 0.$$

has distinct real roots

$$\therefore \Delta > 0.$$

$$(-2)^2 - 4(p-1)(1) > 0$$

$$4 - 4(p-1) > 0$$

$$4 - 4p + 4 > 0$$

$$8 > 4p.$$

$$p < 2 \quad (C).$$

$$7. \quad 3x^2 + 4x + 1 \equiv 3(x+a)^2 + b$$

$$3x^2 + 4x + 1 = 3(x^2 + 2ax + a^2) + b$$

$$3x^2 + 4x + 1 = 3x^2 + 6ax + (3a^2 + b)$$

$$\begin{cases} \therefore 6a = 4 \\ 3a^2 + b = 1 \end{cases} \quad \begin{aligned} \therefore a &= \frac{2}{3} \\ b &= -\frac{1}{3} \end{aligned} \quad (B)$$

$$8. k^2 + kx - (k+1) = 0$$

since 2 is a root.

$$\therefore 2^2 + k(2) - (k+1) = 0$$

$$4 + 2k - k - 1 = 0$$

$$k = -3.$$

$$9. x^2 - 3x + 2 = 0$$

$$\therefore \alpha \cdot \beta = \frac{2}{1} = 2 \quad (\text{A})$$

Method (II).

$$x^2 + kx - (k+1) = 0.$$

let 2 &  $\alpha$  be the roots.

$$\therefore \begin{cases} 2 + \alpha = -k \\ 2\alpha = -(k+1) \end{cases}$$

$$2\alpha = (2 + \alpha) - 1$$

$$\alpha = 1$$

$$\therefore \text{product of roots} = 2 \times 1 = 2 \quad (\text{A})$$

$$9. y = x^2 + 4x + k.$$

touches the x-axis.

For  $y = 0$ ,

$$x^2 + 4x + k = 0.$$

has repeated roots / double roots.

$$\therefore \Delta = 0$$

$$4^2 - 4(1)(k) = 0$$

$$16 - 4k = 0$$

$$4k = 16$$

$$k = 4$$

(C)

$$10. y = a(x+1)^2 + b$$

$$\therefore a < 0$$

(open downwards)

$$\text{vertex} = (-1, b).$$

$$b > 0.$$

$\therefore a \cdot b < 0$ . (I) is true.

For  $x = 0$ ,

$$y = a(0+1)^2 + b$$

$$= a+b$$

$$\therefore y\text{-intercept} = a+b \neq b.$$

$\therefore$  (II) is false.

$$\text{vertex} = (-1, b) \neq (a, b)$$

(III) is false. (A).

$$11. (a^2 + 4a + 4) - (b^2 - 2b + 1)$$

$$= (a+2)^2 - (b-1)^2$$

$$= [(a+2) - (b-1)] \cdot [(a+2) + (b-1)]$$

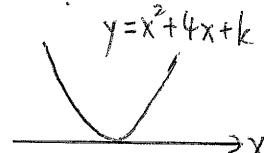
$$= (a-b+3)(a+b+1) \quad (\text{ })$$

$$12. f(x) = (x^2 - 5x - 6) Q(x)$$

$$= (x-6)(x+1) Q(x)$$

$$\therefore f(6) = 0$$

$$\& f(-1) = 0. \quad (\text{C})$$



$$13. \quad (3x+4y) \propto (4x-5y)$$

$$\therefore (3x+4y) = k(4x-5y)$$

where  $k$  is a constant,  $\neq 0$ .

$$3x + 4y = 4kx - 5ky.$$

$$4kx - 3x = 5ky + 4y.$$

$$(4k-3)x = (5k+4)y.$$

$$y = \left(\frac{4k-3}{5k+4}\right)x.$$

$$\therefore y \propto x \quad (\text{B})$$

since  $k$  is a constant,

$\left(\frac{4k-3}{5k+4}\right)$  is also a constant.

$$14. \quad \frac{5a+3b}{a+b} = 3.$$

$$5a+3b = 3a+3b.$$

$$2a = 0.$$

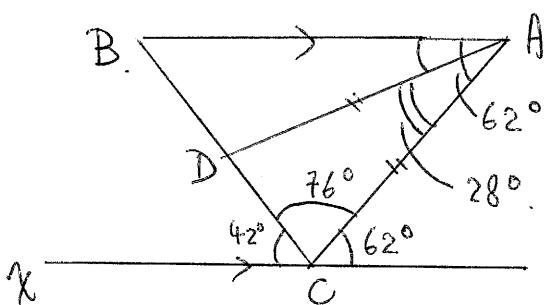
$$a = 0.$$

$$\therefore a+b = a-b.$$

$$\therefore b = -b = 1 < -1.$$

(wrong Qn).

$$15. \quad \begin{array}{c} \text{B} \\ \swarrow \searrow \\ \text{D} \end{array}$$



$$\text{Step 1: } \angle BAC = 62^\circ. \quad \text{P.3}$$

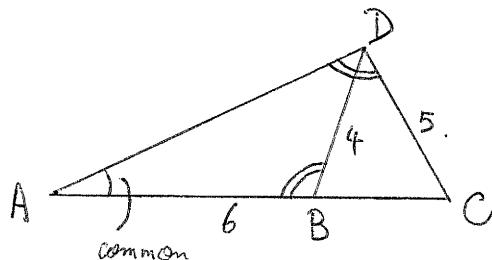
$$\text{Step 2: } \angle ACB = 180^\circ - 62^\circ - 42^\circ \\ = 76^\circ.$$

$$\text{Step 3: } \angle ADC = \angle ACB = 76^\circ.$$

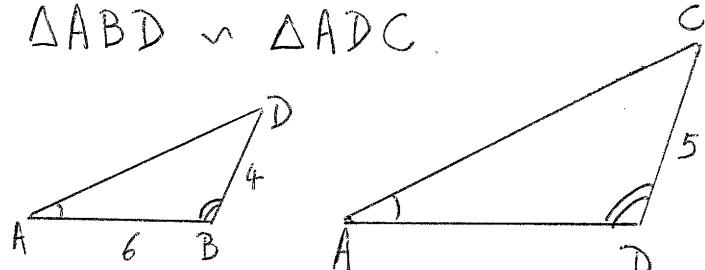
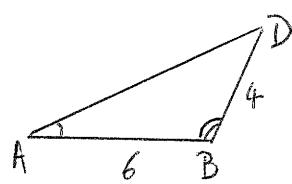
$$\text{Step 4: } \angle DAC = 180^\circ - 76^\circ \times 2 \\ = 28^\circ.$$

$$\text{Step 5: } \angle BAD = 62^\circ - 28^\circ \\ = 34^\circ \quad (\text{D}).$$

16.



$$\triangle ABD \sim \triangle ADC.$$



$$\therefore \frac{AD}{6} = \frac{5}{4}$$

$$AD = 7.5. \quad (\text{B}).$$

$$17. \quad \left[1 + \cos\left(\frac{\pi}{2} - \theta\right)\right] \left[1 - \sin(\pi - \theta)\right]$$

$$= [1 + \sin\theta][1 - \sin\theta]$$

$$= 1 - \sin^2\theta$$

$$= \cos^2\theta. \quad (\text{B}).$$

$$18. \sin x = 2\cos^2 x - 1$$

$$\sin x = 2(1-\sin^2 x) - 1$$

$$\sin x = 2 - 2\sin^2 x - 1$$

$$2\sin^2 x + \sin x - 1 = 0.$$

$$(2\sin x - 1)(\sin x + 1) = 0$$

$$\sin x = \frac{1}{2} \text{ or } -1.$$

$$= 30^\circ, 150^\circ, 270^\circ. (c).$$

19. a, b, c, d, e in A.S.

$$\begin{cases} b = a+d_1 \\ c = a+2d_1 \\ d = a+3d_1 \\ e = a+4d_1 \end{cases} \quad \begin{matrix} \text{where } d_1 \text{ is} \\ \text{the common} \\ \text{difference.} \end{matrix}$$

$$\therefore b + e = 26.$$

$$(a+d_1) + (a+4d_1) = 26.$$

$$2a + 5d_1 = 26 \quad \text{--- (1)}$$

$$a + c + d = 29.$$

$$a + (a+2d_1) + (a+3d_1) = 29.$$

$$3a + 5d_1 = 29 \quad \text{--- (2)}$$

$$(2) - (1)$$

$$a = 3$$

$$\therefore 2(3) + 5d_1 = 26$$

$$5d_1 = 20$$

$$d_1 = 4. \quad (c)$$

$$20. 1 + x + x^2 + \dots = \frac{4}{3}$$

$$a = 1,$$

$$R = x.$$

$$\frac{a}{1-R} = \frac{4}{3}$$

$$\frac{1}{1-x} = \frac{4}{3}$$

$$3 = 4 - 4x$$

$$4x = 1, x = \frac{1}{4} (D)$$

$$21.$$

$$L_1 \times (-2, 0)$$

$$x + 2y - 1 = 0.$$

$$L_2: x + 2y - 1 = 0.$$

$$2y = -x + 1$$

$$y = -\frac{1}{2}x + \frac{1}{2}$$

$$\therefore m_2 = -\frac{1}{2}$$

$$L_1 \perp L_2$$

$$\therefore m_1 \cdot m_2 = -1$$

$$m_1 \cdot (-\frac{1}{2}) = -1$$

$$m_1 = 2.$$

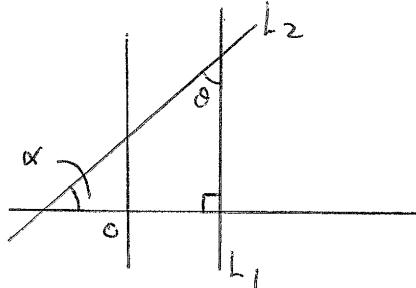
cgt. of  $L_1$

$$y - 0 = 2(x - (-2))$$

$$y = 2x + 4.$$

$$2x - y + 4 = 0. (B)$$

$$22.$$



$$L_2: x - \sqrt{3}y + 4 = 0$$

$$\sqrt{3}y = x + 4$$

$$y = \frac{1}{\sqrt{3}}x + \frac{4}{\sqrt{3}}$$

$$\therefore m_2 = \frac{1}{\sqrt{3}}$$

$$\tan \alpha = \frac{1}{\sqrt{3}}$$

$$\alpha = 30^\circ$$

$$\therefore \theta = 60^\circ. (C)$$

P.4.

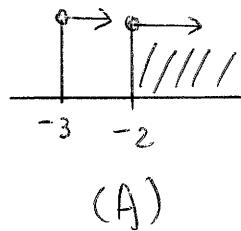
$$23. \begin{cases} -x < 3 \\ \frac{2x+4}{4} > -2 \end{cases}$$

$$\begin{cases} -3 < x \\ 2x+4 > -8 \end{cases}$$

$$\begin{cases} x > -3 \\ 2x > -4 \end{cases}$$

$$\begin{cases} x > -3 \\ x > -2 \end{cases}$$

$$\therefore x > -2$$



(A)

$$24. (1-2x)(x+1) \geq 1-2x$$

Method (I)

$$(1-2x)(x+1) - (1-2x) \geq 0$$

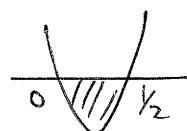
$$(1-2x)(x+1-1) \geq 0$$

$$(1-2x)x \geq 0$$

$$-(2x-1)x \geq 0$$

$$x(2x-1) \leq 0$$

$$0 \leq x \leq \frac{1}{2}$$



Method (II)

$$(1-2x)(x+1) \geq 1-2x$$

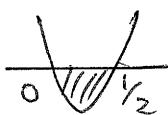
$$x-2x^2+1-2x \geq 1-2x$$

$$-2x^2+x \geq 0$$

$$2x^2-x \leq 0$$

$$x(2x-1) \leq 0$$

$$0 \leq x \leq \frac{1}{2}$$



(B)

$$25. \begin{aligned} & P(\text{2 shoes are in pair}) \\ & = P(A.A \text{ or } B.B \text{ or } C.C) \\ & = \frac{2}{6} \cdot \frac{1}{5} + \frac{2}{6} \cdot \frac{1}{5} + \frac{2}{6} \cdot \frac{1}{5} \\ & = \frac{1}{15} + \frac{1}{15} + \frac{1}{15} \\ & = \frac{1}{5} \end{aligned}$$

(C)

$$26. \begin{array}{c} \begin{pmatrix} 3B \\ 2W \end{pmatrix} \\ \text{bag A.} \\ \text{Method (I)} \end{array} \quad \begin{array}{c} \begin{pmatrix} 3W \\ 4B' \end{pmatrix} \\ \text{bag B.} \end{array}$$

$P(\text{they are different in colour})$

$$\begin{aligned} & = 1 - P(\text{they are same colour}) \\ & = 1 - P(W.W) \\ & = 1 - \frac{2}{5} \cdot \frac{3}{7} \\ & = \frac{29}{35} \end{aligned}$$

(D)

Method (II).

$P(\text{they are different in colour})$

$$\begin{aligned} & = P(BW \text{ or } BB' \text{ or } WB') \\ & = \frac{3}{5} \cdot \frac{3}{7} + \frac{3}{5} \cdot \frac{4}{7} + \frac{2}{5} \cdot \frac{4}{7} \\ & = \frac{9+12+8}{35} = \frac{29}{35} \end{aligned}$$

(D)

$$27. \bar{x} = 2.83.$$

median = 3.

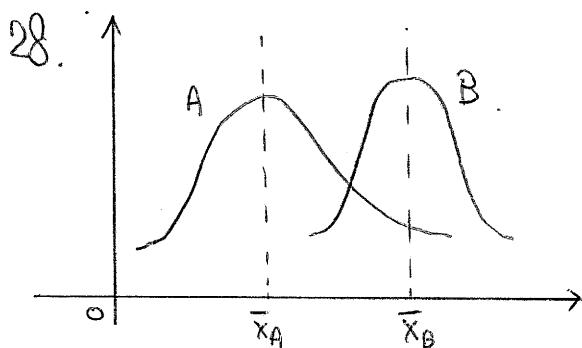
mode = 2.

(I) median >  $\bar{x}$  (false)

(II) mode > median (false)

(III) mode > mean (false).

(A)



(I)  $\bar{x}_B > \bar{x}_A$  (true)

(II) median of B > median of A (true)

(III)  $s_B > s_A$  (false) (B)

$$28. \begin{cases} y = \sin x + x. & \text{--- } \textcircled{1} \\ x + 3y - 2 = 0 & \text{--- } \textcircled{2} \end{cases}$$

sub \textcircled{1} into \textcircled{2} (remove " $y$ ").

$$x + 3(\sin x + x) - 2 = 0$$

$$3\sin x + 4x - 2 = 0. \quad (\text{C}).$$

$$30. \begin{cases} T(3) = 4 \\ T(5) = 20 \end{cases}$$

$$\begin{cases} aR^2 = 4 & \text{--- } \textcircled{1} \\ aR^4 = 20 & \text{--- } \textcircled{2} \end{cases}$$

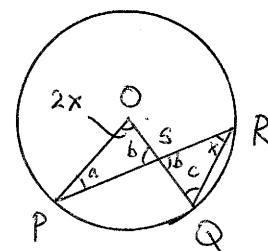
$$P.6. \quad \textcircled{1} \quad \frac{aR^4}{aR^2} = \frac{20}{4} \\ R^2 = 5 \\ R = \pm \sqrt{5}.$$

$$\text{from } \textcircled{1} \quad aR^2 = 4$$

$$a(5) = 4$$

$$a = \frac{4}{5}. \quad (\text{B}).$$

31.



$$\text{let } \angle PQR = x.$$

$$\angle POQ = 2x.$$

$$a + b + 2x = 180^\circ. \quad \text{--- } \textcircled{1}$$

$$b + c + x = 180^\circ \quad \text{--- } \textcircled{2}$$

$$x = 180^\circ - b - c.$$

$$\therefore a + b + 2(180^\circ - b - c) = 180^\circ.$$

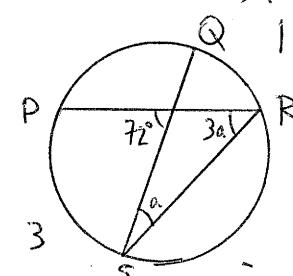
$$a + b + 360^\circ - 2b - 2c = 180^\circ$$

$$a = b + 2c - 180^\circ. \quad (\text{D}).$$

32.

$$3a + a = 72^\circ.$$

(ext. Ls. of  $\triangle$ )



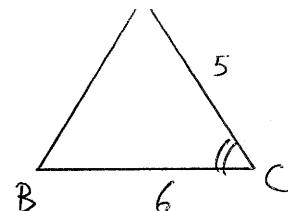
$$4a = 72^\circ$$

$$a = 18^\circ. \quad (\text{A}).$$

$$33. \tan C = \frac{4}{3}$$

$$\therefore \sin C = \frac{4}{5}$$

$$\cos C = \frac{3}{5}$$



$$AB^2 = 5^2 + 6^2 - 2(5)(6) \cdot \cos C$$

$$AB^2 = 25 + 36 - 60\left(\frac{3}{5}\right)$$

$$AB^2 = 25$$

$$AB = 5. \quad (\text{D})$$

34.

$$\text{Let. } PQ = QR = x.$$

$$\tan 30^\circ = \frac{x}{OR}$$

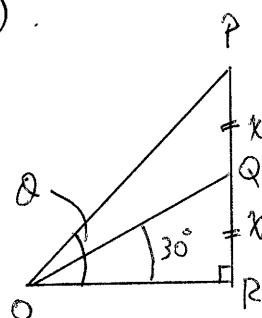
$$\frac{1}{\sqrt{3}} = \frac{x}{OR}$$

$$OR = \sqrt{3}x.$$

$$\tan \alpha = \frac{2x}{\sqrt{3}x}$$

$$= \frac{2}{\sqrt{3}}$$

$$\alpha = 49.1^\circ. \quad (\text{B}).$$



35. perimeter of sector = perimeter of square

$$s + 2a = 4a.$$

$$s = 2a.$$

$$\therefore \omega = \frac{s}{a} = \frac{2a}{a} = 2 \text{ radian.}$$

$$\frac{\text{area of sector}}{\text{area of square}} = \frac{\frac{1}{2}a^2(2)}{a^2}$$

$$= 1. \quad (\text{A}).$$

$$36. \text{ vol. of hemisphere} = \text{vol. of cone.}$$

$$\frac{1}{2} \times \frac{4}{3} \pi r^3 = \frac{1}{3} \pi r^2 h.$$

$$\frac{2}{3}r = \frac{1}{3}h.$$

$$2r = h.$$

$$\frac{r}{h} = \frac{1}{2}$$

$$\therefore r:h = 1:2. \quad (\text{C}).$$

P.f.

$$37. \log y = n \log x + C.$$

$$\log y = n \log x + \log 10^c$$

$$\log y = \log x^n + \log 10^c$$

$$\log y = \log x^n \cdot 10^c.$$

$$y = 10^c \cdot x^n. \quad (\text{A}).$$

$$38. \frac{\sqrt{a}}{\sqrt{a}-\sqrt{b}} - \frac{\sqrt{b}}{\sqrt{a}+\sqrt{b}}$$

$$= \frac{\sqrt{a}}{\sqrt{a}-\sqrt{b}} \times \frac{\sqrt{a}+\sqrt{b}}{\sqrt{a}+\sqrt{b}} - \frac{\sqrt{b}}{\sqrt{a}+\sqrt{b}} \times \frac{\sqrt{a}-\sqrt{b}}{\sqrt{a}-\sqrt{b}}$$

$$= \frac{a + \sqrt{ab}}{a - b} - \frac{\sqrt{ab} - b}{a - b}$$

$$= \frac{(a + \sqrt{ab}) - (\sqrt{ab} - b)}{a - b}$$

$$= \frac{a + b}{a - b}. \quad (\text{B}).$$

$$39. x = \frac{k y^2}{z}, \quad k \neq 0.$$

$$x_1 = \frac{k y_1^2}{z_1}$$

$$\begin{cases} y_1 = 1.2y \\ z_1 = 0.8z \end{cases}$$

$$x_1 = \frac{k (1.2y)^2}{0.8z}$$

$$x_1 = \frac{k y^2}{z} (1.8)$$

31. (cont'd).

$$X_1 = 1.8x.$$

% change

$$= \frac{X_1 - x}{x} \cdot 100\%$$

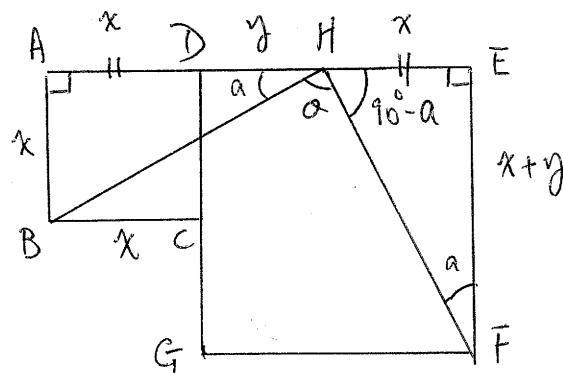
$$= \frac{1.8x - x}{x} \cdot 100\%$$

$$= \frac{0.8x}{x} \cdot 100\%$$

$$= (0.8)(100\%) = 80\%.$$

$x$  is increased in 80%. (D).

40.



Let. AD be  $x$  & DH be  $y$ .

$$\therefore AB = AD = HE = x.$$

$$\therefore DE = x + y.$$

$$\& EF = DE = x + y.$$

$$AH = x + y = EF.$$

$\therefore$  (II) is true.

But  $BC \neq DH$

(I) is false.

since  $\triangle AHB \cong \triangle EHF$ .

$$\therefore \angle AHB = \angle EHF = \alpha.$$

$$\therefore \angle EHF = 180^\circ - 90^\circ - \alpha \\ = 90^\circ - \alpha.$$

$$\alpha + \theta + (90^\circ - \alpha) = 180^\circ \quad \text{P.8}$$

$$\theta + 90^\circ = 180^\circ$$

$$\theta = 90^\circ.$$

$\therefore$  (II) is true. (D).

$$41. \sin \alpha = \frac{-3}{5}$$

$$x^2 + (-3)^2 = 5^2$$

$$x^2 = 25 - 9$$

$$x = \pm 4.$$

since  $x < 0$ ,  $\therefore x = -4$ .

$$\cos \alpha = \frac{-4}{5} \quad \& \quad \tan \alpha = \frac{-3}{-4} = \frac{3}{4}.$$

$$\therefore \frac{\sin \alpha + 3 \cos \alpha}{\tan \alpha}$$

$$= \frac{-3/5 + 3(-4/5)}{3/4}$$

$$= \frac{-3}{3/4} = -4. \quad (\text{C}).$$

$$42. \frac{A_2}{A_3} = \left( \frac{l_2}{l_3} \right)^2$$

$$\frac{1}{3} = \left( \frac{l_2}{l_3} \right)^2$$

$$\frac{l_2}{l_3} = \frac{1}{\sqrt{3}}.$$

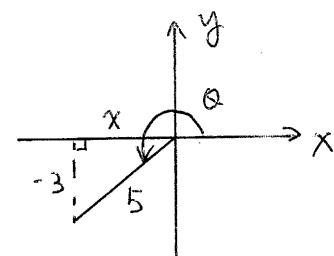
$$\therefore l_2 = l_3 = 1 = \sqrt{3}.$$

$$\frac{V_3}{V_1} = \left( \frac{l_3}{l_1} \right)^3$$

$$\frac{8}{1} = \left( \frac{l_3}{l_1} \right)^3.$$

$$\frac{l_3}{l_1} = \frac{2}{1}$$

$$l_3 : l_1 = 2 : 1$$



$$42) l_2 = l_3 \quad | = \sqrt{3} \\ \frac{l_3 = l_1}{l_2 : l_3 : l_1} = \frac{2 = 1}{2 : 2\sqrt{3} : \sqrt{3}}.$$

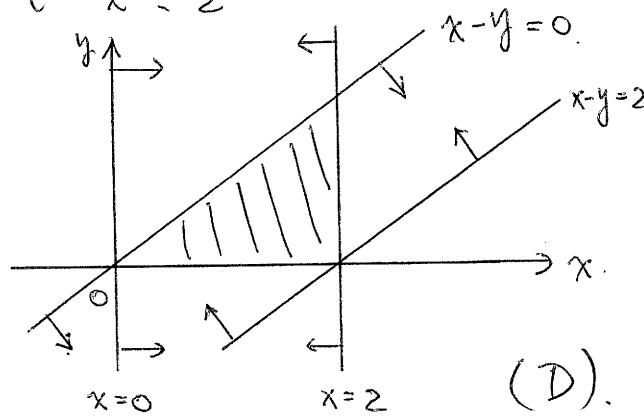
$$\frac{l_2}{l_1} = \frac{2}{\sqrt{3}}.$$

$$\begin{aligned} \frac{A_1}{A_2} &= \left(\frac{l_1}{l_2}\right)^2 \\ &= \left(\frac{\sqrt{3}}{2}\right)^2 = \frac{3}{4}. \end{aligned}$$

$$\therefore A_1 : A_2 = 3 : 4 \quad (\text{B}).$$

$$43 \quad \begin{cases} 0 \leq x-y \leq 2 \\ 0 \leq x \leq 2. \end{cases}$$

$$\begin{cases} x-y \geq 0 \\ x-y \leq 2 \\ x \geq 0 \\ x \leq 2 \end{cases}$$



(D).

| $x$  | $f(x)$ |
|------|--------|
| 0.6  | +0.26  |
| 0.7  | +0.06  |
| 0.75 | -0.02  |
| 0.8  | -0.10  |
| 1    | -0.46  |

$$\therefore 0.7 < x < 0.75.$$

$$\therefore x = 0.7 \text{ (corr. to 1 d.p.)} \quad (\text{B})$$

$$45. \quad (x+1)^2 - 4(x+1) + 2 = 0. \quad \text{P. 9}$$

Method (I).

$\alpha, \beta$  are the roots.

$$\begin{cases} (\alpha+1)^2 - 4(\alpha+1) + 2 = 0 \\ (\beta+1)^2 - 4(\beta+1) + 2 = 0. \end{cases}$$

$$\text{let } y = \alpha+1 \quad \& \quad y = \beta+1.$$

$$\therefore y^2 - 4y + 2 = 0$$

$\therefore (\alpha+1) \& (\beta+1)$  are the roots  
(A).

Method (II).

$$(x+1)^2 - 4(x+1) + 2 = 0$$

$$x^2 + 2x + 1 - 4x - 4 + 2 = 0$$

$$x^2 - 2x - 1 = 0$$

$$\therefore \alpha + \beta = \frac{-(-2)}{1} = 2$$

$$\alpha \cdot \beta = \frac{-1}{1} = -1.$$

$$\begin{aligned} \text{sum of roots} &= (\alpha+1) + (\beta+1) \\ &= (\alpha+\beta) + 2 \\ &= 2 + 2 = 4. \end{aligned}$$

$$\begin{aligned} \text{product of roots} &= (\alpha+1) \cdot (\beta+1) \\ &= \alpha\beta + \alpha + \beta + 1 \\ &= -1 + 2 + 1 \\ &= 2. \end{aligned}$$

$\therefore$  the required eqt. in  $y$  is

$$y^2 - 4y + 2 = 0 \quad (\text{A}).$$

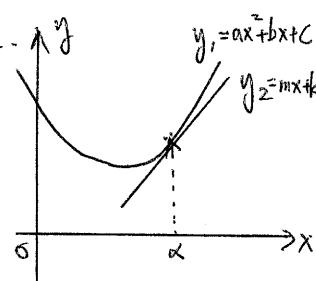
46.  $ax^2 + (b-m)x + (c-k) > 0$

$(ax^2 + bx + c) - mx - k > 0$

$ax^2 + bx + c > mx + k$

$y_1 > y_2$

since  $\vee$  is always greater than  $\backslash$   
except.,  $x = \alpha$ .



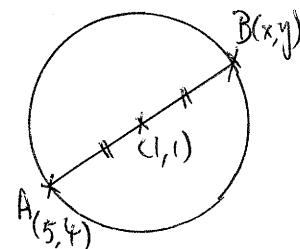
$\therefore$  All real values of  $x$  except for  $x = \alpha$ . (D).

47.  $x^2 + y^2 - 2x - 2y - 23 = 0$ .

centre =  $(1, 1)$ .

Let. B be  $(x, y)$

$$\left\{ \begin{array}{l} 1 = \frac{5+x}{2} \\ 1 = \frac{4+y}{2} \end{array} \right.$$



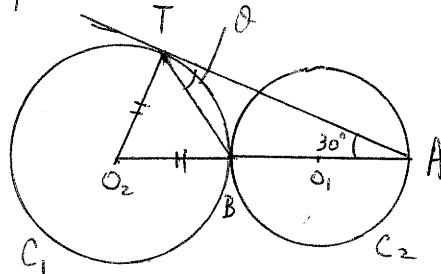
$$\left\{ \begin{array}{l} 5+x=2 \\ 4+y=2 \end{array} \right. \therefore \left\{ \begin{array}{l} x=-3 \\ y=-2 \end{array} \right.$$

$\therefore B = (-3, -2)$ . (A).

$$\begin{aligned} 48. \frac{\frac{1}{x^3} - \frac{1}{y^3}}{\frac{1}{x} - \frac{1}{y}} &= \frac{\frac{1}{x^3 y^3} (y^3 - x^3)}{\frac{1}{x y} (y - x)} \\ &= \frac{1}{x^2 y^2} \cdot \frac{(y^3 - x^3)}{(y - x)} \\ &= \frac{1}{x^2 y^2} \cdot \frac{(y-x)(y^2 + xy + x^2)}{(y-x)} \\ &= \frac{y^2 + xy + x^2}{x^2 y^2} \\ &= \frac{1}{x^2} + \frac{1}{x y} + \frac{1}{y^2} \end{aligned}$$

(C)

47.



P.10

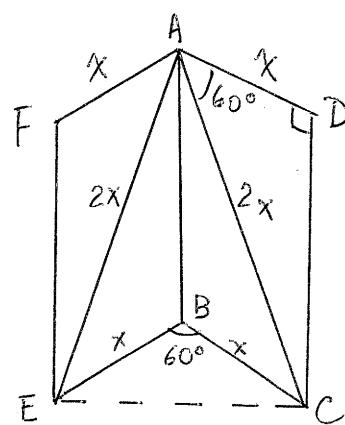
$\angle O_2 TA = 90^\circ$

$\angle A O_2 T = 90^\circ - 30^\circ = 60^\circ$ .

$\angle O_2 TB = \angle O_2 BT = \frac{180^\circ - 60^\circ}{2} = 60^\circ$ .

$\therefore O = 90^\circ - 60^\circ = 30^\circ$ . (B)

50.



Let AD be x.

$\therefore AD = AF = BC = BE = x$ .

$$\cos 60^\circ = \frac{AD}{AC}$$

$$\frac{1}{2} = \frac{x}{AC}$$

$\therefore AC = 2x$ . ( $\because AE = AC = 2x$ )

In  $\triangle BCE$ ,

$$\begin{aligned} CE^2 &= x^2 + x^2 - 2(x)(x) \cos 60^\circ \\ &= x^2 + x^2 - 2x^2 \left(\frac{1}{2}\right) \\ &= x^2 \end{aligned}$$

$\therefore CE = x$ .

In  $\triangle ACE$ .

$$x^2 = (2x)^2 + (2x)^2 - 2(2x)(2x) \cos LCAE$$

$$x^2 = 4x^2 + 4x^2 - 8x^2 \cos LCAE$$

$$8x^2 \cos LCAE = 7x^2$$

$$\cos LCAE = \frac{7}{8}$$

$$LCAE = 28.96^\circ \quad (\text{A})$$

$$= 29^\circ \text{ (nearest degree)}$$

51. 4, a, b, 25 in G.S.

$$T(1) = a' = 4$$

$$T(2) = a = a'R = 4R$$

$$T(3) = b = a'R^2 = 4R^2$$

$$T(4) = 25 = a'R^3 = 4R^3$$

$$\therefore 4R^3 = 25 \quad \text{--- (1)}$$

$$4R^2 = b \quad \text{--- (2)}$$

$$4R = a \quad \text{--- (3)}$$

$$\therefore \log a + \log b$$

$$= \log a \cdot b$$

$$= \log (4R)(4R^2)$$

$$= \log 4 \cdot (4R^3)$$

$$= \log 4(25)$$

$$= \log 100$$

$$= 2 \quad (\text{C})$$

52.

P. 11

$$x^2 + y^2 - 6x - 10y + 9 = 0$$

For  $y = 0$ ,

$$x^2 - 6x + 9 = 0$$

$$(x-3)^2 = 0$$

$$x = 3$$

$$\therefore P = (3, 0)$$

For  $x = 0$ ,

$$y^2 - 10y + 9 = 0$$

$$(y-9)(y-1) = 0$$

$$y = 9 \text{ or } 1$$

$$\therefore Q = (0, 1) \quad \& \quad R = (0, 9)$$

area of  $\triangle PQR$

$$= \text{area of } \triangle OPR - \text{area of } \triangle OPQ$$

$$= \frac{1}{2}(3)(9) - \frac{1}{2}(3)(1)$$

$$= \frac{27}{2} - \frac{3}{2} = 12 \quad (\text{D})$$

53.

$P$  (the problem can be solved)

$= P$  (at least one of them solve the problem)

$$= 1 - P(J' \cdot P' \cdot N')$$

$$= 1 - \left(\frac{2}{3}\right) \cdot \left(\frac{3}{4}\right) \cdot \left(\frac{4}{5}\right)$$

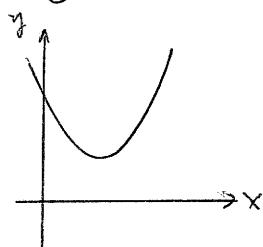
$$= 1 - \frac{2}{5} = \frac{3}{5} \quad (\text{B})$$

$$54. ax^2 - (a+2)x + 1 > 0.$$

for all real value of  $x$ .

$$\therefore \Delta < 0.$$

$$[-(a+2)]^2 - 4a^2(1) < 0$$



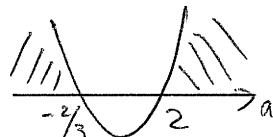
$$(a+2)^2 - 4a^2 < 0$$

$$a^2 + 4a + 4 - 4a^2 < 0.$$

$$3a^2 - 4a - 4 > 0.$$

$$(3a+2)(a-2) > 0$$

$$a < -\frac{2}{3} \text{ or } a > 2.$$



(D)

### 5.5 Mock Exam. (2001 - 2002)

- |      |      |      |       |       |      |       |       |
|------|------|------|-------|-------|------|-------|-------|
| 1. C | 6 C  | 11 D | 16 B  | 21 B  | 26 D | 31 D  | 36 C  |
| 2 D  | 7 B. | 12 C | 17 B. | 22 C  | 27 A | 32 A. | 37 A  |
| 3 D  | 8 A  | 13 B | 18 C  | 23 A  | 28 B | 33 D  | 38 B. |
| 4 B  | 9 C  | 14   | 19 C  | 24 B. | 29 C | 34 B  | 39 D  |
| 5 A  | 10 A | 15 D | 20 D  | 25 C  | 30 B | 35 A. | 40 D. |

41 C    46 D    51 C

42 B    47 A    52 D

43 D    48 C    53 B.

44 B    49 B    54 D.

45 A    50 A