

1. (i) Total charge =  $ALne$   
 (ii) Time taken =  $L/v$   
 (iii) current  $I = \text{Total charge}/\text{time}$   
 $= ALne/(L/v) = nAve$   
 (iv)  $v = I/nAe$   
 $= 1/(9 \times 10^{28})(1 \times 10^{-6})(1.6 \times 10^{-19})$   
 $= 6.9 \times 10^{-5} \text{ m/s}$
  
3. (a)  $E = Ir + IR$   
 $I = E/(R+r)$   
 Because  $V = IR = R E/(R+r)$   
 Hence  $E/V = 1 + r(1/R)$   
 $1/R = (E/r)(1/V) - (1/r)$   
 (b)  $r = 0.4 \Omega, E = 1.5 \text{ V}$
  
4. (a) Terminal A should be "positive", because it is a charging process.  
 (b)  $(2.4 - 12.6) = 5(1+R+0.1)$   
 Therefore  $R = 1.18 \Omega$   
 (c) When  $R = 0.9 \Omega$ ,  
 $I = (2.4-12.6)/(0.9+1+0.1)$   
 $= 5.7 \text{ A}$   
 $V_1 = \epsilon_1 - I r_1 = 24 - 5.7(1) = 18.3 \text{ V}$   
 $V_2 = \epsilon_2 - I r_2 = 12.6 + 5.7(0.1) = 13.17$
  
5. (a) (i)  $\frac{R}{l} = \frac{4\rho}{\pi d^2}$   
 (ii) Slope =  $4\rho/\pi$   
 $= (0.045 / 2 \times 10^6)$   
 Therefore,  $\rho = 1.77 \times 10^{-8} \Omega \text{ m}$   
 (b) (i)  $P = IV, I = 3000 / 240 = 12.5 \text{ A}$   
 (ii) From graph  $R/l = 0.005$  at  $d = 1.78 \text{ mm}$   
 $R = 10 \times 0.005 = 0.05 \Omega$   
 (iii)  $P = I^2 R = (12.5)^2 \times 0.05 = 7.81 \text{ W}$   
 (iv) Thinner wire results in higher resistance.  
 -It means a lower portion of voltage drops across the heating element.  
 (heater works below its rated power).
  
5. Originally  $R = \rho(l)/A$   
 Now  $R' = \rho(l_1)/4A = \rho(l/4)/4A$   
 $= 1/16 (\rho(l)/A) = R/16$   
 Therefore current is increased to  
 $16 \times 0.1 \text{ A} = 1.6 \text{ A}$
  
6. Consider same length and resistance,  
 Since  $R = \rho(l)/A$ , therefore  $R/l = \rho/A$   
 $\rho_{\text{cu}}/A_{\text{cu}} = \rho_{\text{Al}}/A_{\text{Al}}$   
 Cross-sectional area for Al cable is 1.6 times greater  
 However, mass = volume x density  
 $= A \times l \times \sigma$   
 Therefore, mass of copper is  $3.2/1.6 = 2$  times that of aluminium.  
 Therefore, cost for Aluminium would be half that of copper.  
 Because the line is lighter, the pylons and insulators that support it can be built more cheaply. However, extra thickness leads to problems of larger forces on the line in high winds.
  
7. (a) Figure 1 is impossible, B is on open circuit,  $V_{BC} = 0$   
 Figure 2 is impossible, B is on open circuit,  $V_{AB} = 0$   
 Figure 3 is impossible, A and B is short-circuited. Therefore  $V_{AB} = 0$   
 Figure 5 is impossible, A and C is short-circuited. Therefore  $V_{AC} = 0$   
 The possible arrangement are Figure 4 and Figure 6.  
 (b) (i) Figure 6 is impossible, C is on open circuit,  $V_{BC} = 0$ .  
 (ii)  $X = 10\Omega, Y = 20 \Omega, Z = 30 \Omega$

8. When  $K_2$  is closed, voltmeter reading should be 8 Volts.
12. (a) The resistance of the voltmeter  $R$  is given by  $60 / (40R / (40 + R) + 60) \times 4 = 2.5$ ,  $R = 360 \Omega$
- (b) With voltmeter connection, equivalent resistance across  $Y'Z'$  is  $(400)(360) / 760 = 189.5 \Omega$   
Hence voltmeter reading is  $189.5 / (189.5 + 600) \times 4 \text{ V} = 0.96 \text{ V}$   
Voltmeter should not be used in measuring the p.d. across resistance comparable to voltmeter resistance.
13. (a) When  $S$  is open, voltmeter reading =  $100 / (100 + 100) \times 12 \text{ V} = 6 \text{ V}$   
When  $S$  is closed, voltmeter reading =  $50 / (100 + 50) \times 12 \text{ V} = 4 \text{ V}$
14. The e.m.f.  $\epsilon$  of the source is given by  $400 / (400 + 2000) \times \epsilon = 10$   
e.m.f.  $\epsilon = 60 \text{ V}$   
When voltmeter is not used, p.d. across  $2000 \Omega$  is  $2000 / (500 + 2000) \times 60 \text{ V} = 48 \text{ volts}$
15. Equivalent resistance across voltmeter is  $5000 \times 2000 / 7000 = 10^4 / 7 \Omega$   
Total resistance of the circuit is  $10^4 / 7 + 5000 = 45000 / 7 \Omega$   
Therefore, voltmeter reading is  $(10000 / 7) / (45000 / 7) \times 10 \text{ V} = 20 / 9 \text{ V}$
16. Use  $\Sigma \epsilon = \Sigma IR$   
 $(6 - 4) = I_1 (2)$ ,  $I_1 = 1 \text{ A}$   
 $4 = I_2 (2)$ ,  $I_2 = 2 \text{ A}$
17. (i) For parallel connection, power dissipated for  $L_1$  is  $12 \text{ W}$  and  $L_2$  is  $24 \text{ W}$  and total power is  $36 \text{ W}$ .
- (ii) Resistance of  $L_1$  is  $V^2 / P = 12 \Omega$   
Resistance of  $L_2$  is  $V^2 / P = 6 \Omega$
- p.d. across  $L_1$  is  $12 \times 12 / 18 = 8 \text{ V}$  and so  
p.d. across  $L_2$  is  $4 \text{ V}$   
Therefore, power dissipated in  $L_1$  is  $V^2 / R = 16 / 3 \text{ W}$   
power dissipated in  $L_2$  is  $V^2 / R = 8 / 3 \text{ W}$   
Hence total power is  $8 \text{ W}$ .
18. (a)  $P_R = (2 / (2 + R))^2 R = 4R / (2 + R)^2$   
(plot graph)
- (b)  $\eta = \text{output power} / \text{input power} = R / (R + 2) \times 100\%$  (plot graph)
- (c)  $\eta = i^2 R / i E = i R / E = \dots = R / (R + 2)$   
p.d. =  $i R = (2 / (2 + R)) R = 2R / (2 + R)$   
p.d. =  $2 \times \eta = 1.5 \text{ V}$  when  $\eta = 0.75$